Contents

Preface				
Pa	rt I	Introduction	1	
1		e Growth of Meta-Analysis and Implications for Methodolog atroversies	gical 3	
2	Basi	ic Steps of Meta-Analysis and the Emergence of Approaches	9	
	2.1	Basic Steps of Meta-Analysis	9	
	2.2	On the Emergence of Approaches	14	
Pa	rt II	Statistical Methods of Meta-Analysis	17	
3	Effect Sizes		19	
	3.1	Correlation Coefficients as Effect Sizes	20	
	3.2	Standardized Mean Differences as Effect Sizes	28	
	3.3	Conversion of Effect Sizes	30	
4	Gen	neral Frameworks of Meta-Analysis	33	
	4.1	Fixed Effects Model	35	
	4.2	Random Effects Model	39	
	4.3	Mixture Models	42	
	4.4	Hierarchical Linear Models	45	
	4.5	Classes of Situations for the Application of Meta-Analysis	48	
5	Stat	tistical Approaches to Meta-Analysis	55	
	5.1	Hedges and Olkin	56	
		5.1.1 Procedures for <i>r</i> as Effect Size	57	
		5.1.2 Procedures for <i>d</i> as Effect Size	59	
	5.2	Rosenthal and Rubin	61	
	5.3	Hunter and Schmidt	62	
	5.4	Refined Approaches	70	
		5.4.1 DerSimonian-Laird	71	

X CONTENTS

	5.5	5.4.2 Olkin and Pratt Consequences of Choosing an Approach: Different Estimated	72 d	
	c ic	Parameters	75	
	5.6	Comparisons of Approaches: Statistical Procedures	82	
6	Sun	nmary of Statistical Part	87	
Part III Evaluation of Statistical Approaches: A Monte-Carlo Study				
7	Aim	ns, Design, and Implementation	93	
	7.1	Genera] Aims and Procedure	94	
	7.2	General Expectations and Predictions for the Results	95	
	7.3	Distributions in the Universe of Studies	100	
	7.4	Parameters	102	
	7.5	Drawing Random Correlation Coefficients	105	
		7.5.1 Approximations to the Sampling Distribution of <i>r</i>	106	
		7.5.2 Evaluation of the Approximations	109	
	7.6	Details of Programming	114	
	7.7	Summary	114	
8	Res	ults	115	
	8.1	Preliminaries	115	
	8.2	Estimation of the Mean Effect Size in the Universe of Studies	117	
		8.2.1 Bias	118	
		8.2.1.1 Homogeneous Situation ©!	118	
		8.2.1.2 Heterogeneous Situation $$	123	
		8.2.1.3 Heterogeneous Situation e ₃	130	
		8.2.2 Relative Efficiency	134	
	8.3	Significance Tests for the Mean Effect Size: Type I Errors and		
	• •	Power	137	
	8.4	Confidence Intervals	148	
	8.5	Homogeneity Tests	158	
		8.5.1 Homogeneity Tests Based on the Q-Statistic	159	
		8.5.1.1 Homogeneous Situation 6j: Type I Errors	159	
		8.5.1.2 Heterogeneous Situations $O2^{an}d < 5_3$: Power	161	
		8.5.2 The Hunter-Schmidt Approach to the Test of Homogene ity: The 75%- and 90%-rule	164	
	8.6	Estimation of Heterogeneity Variance	170	
		8.6.1 Homogeneous Situation &	171	
		8.6.2 Heterogeneous Situations $@2$ and 6_3	175	

Part IV Putting It All Together	181		
9 Synopsis of Statistical Methods and Monte Carlo Study Results	183		
10 Discussion and Conclusions			
Nomenclature			
References			
Appendices			
Appendix A Beta Distributions in the Universe of Effect Sizes	217		
Appendix B Annotated Mathematica Notebook	223		
Appendix C Tables of Results	229		
Author Index			
Subject Index			